

# Is Inflation Default? The Role of Information in Debt Crises

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# Sovereign Debt and Local-Currency Debt

- Countries that borrow in their own currency more resilient to debt crises
  - ▶ High-debt countries: Japan vs. Italy
  - ▶ High-deficit countries: UK vs. Spain
- Local-currency government bond prices react less to bad news

# A Puzzle

- The ability to print money avoids default risk...
  - ⇒ Interest rates do not jump in anticipation of default
- ...but printing money will cause inflation
  - ⇒ Interest rates should jump in anticipation of inflation

However

- Inflation adjusts more slowly (at least in developed economies)
- Sovereign spreads move very fast, onset of rollover crises is sudden

# Our Story

- Debt crises require a certain amount of coordination
- With foreign-currency debt, anticipate spike in default spreads  
⇒ coordination among **bondholders**
- With domestic-currency debt, anticipate escalation of inflation expectations  
⇒ coordination among **price setters**
- Price setters less precisely informed about gov't finances  
⇒ **Information frictions** underlie differential response of bond prices to shocks

# Model, Timing and Actions

$t = 1$

- Govt sells 1 unit of debt at price  $q_1$
- to bond traders, prior + private signal on  $s$  (precision  $\beta_1$ )

$t = 2$

- bond traders re-sell bonds at price  $q_2$
- to new bond traders (€), or to workers through cash (¥)
  - ▶ prior + private signal on  $s$  (precision  $\beta_2 > \beta_1$ )

$t = 1, 2 \rightarrow$  additional, random noise-agents demand  $\epsilon_t$

$t = 3$

- If  $s \geq \hat{s}$ , govt repays
- If  $s < \hat{s}$ , govt defaults/ inflates by  $1 - \theta$

# Equilibrium Prices

State variable  $z_t = s + \epsilon_t$

$t = 2$

- equilibrium price of debt/money

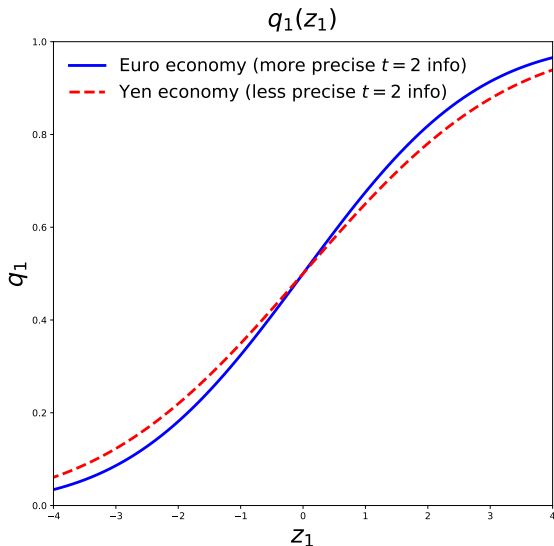
$$q_2(z_2) = \theta + (1 - \theta)\Phi\left(\frac{(1 - w_S)\mu_0 + w_S z_2 - \hat{s}}{\sigma_S}\right)$$

$t = 1$

- equilibrium price of debt

$$q_1(z_1) = \theta + (1 - \theta)\Phi\left[\frac{\mu_0 - \hat{s}}{\sqrt{w_S^2 \sigma_{S|B}^2 + \sigma_S^2}} + \frac{w_S w_B}{\sqrt{w_S^2 \sigma_{S|B}^2 + \sigma_S^2}}(z_1 - \mu_0)\right]$$

# Comparative Statics (more precise info = higher $\beta_2$ )



## What if there is Recall of the First-Period Price?

Same payoffs, but different information set for  $t = 2$  agents

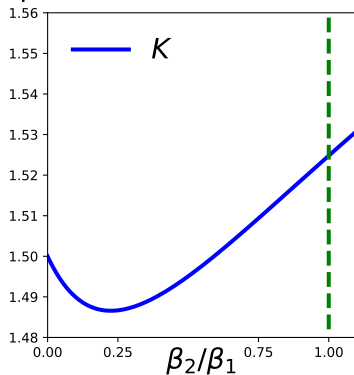
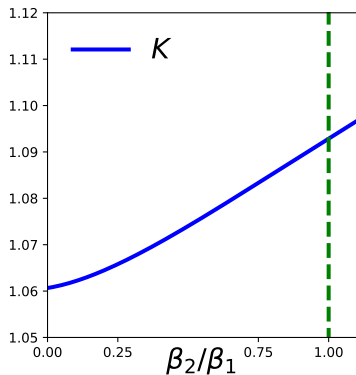
- $z_1$  new source of common knowledge with  $t = 1$  traders



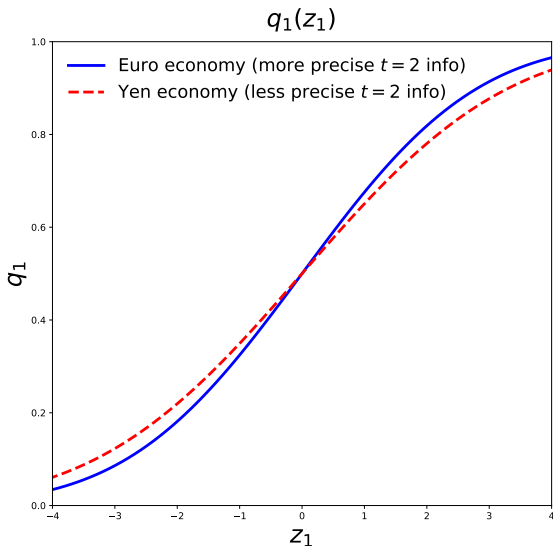
# Comparative Statics

$$q_1(z_1) = \theta + (1 - \theta)\Phi \left[ \frac{\mu_0 - \hat{s}}{\sqrt{w_{2,S}^2 \sigma_{S|B}^2 + \sigma_S^2}} + \underbrace{\left( \frac{w_{1,S} + w_{2,S} w_B}{\sqrt{w_{2,S}^2 \sigma_{S|B}^2 + \sigma_S^2}} \right)}_K (z_1 - \hat{s}) \right]$$

## $t = 1$ Price Responsiveness



# Single Crossing Again

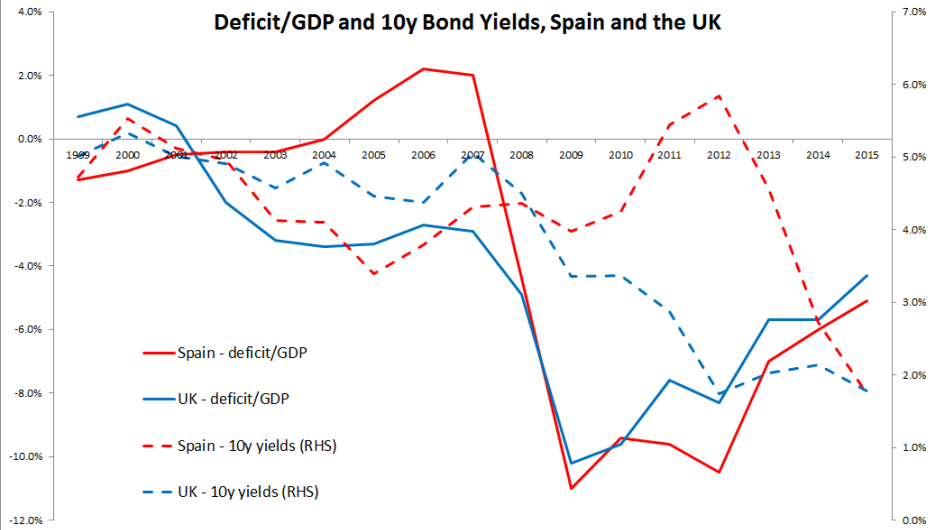


# Conclusion

- Heterogeneity of information has important implications for debt management
- We have shown insurance role of domestic-currency debt
- Next step: optimal theory of currency denomination (study of effects on ex ante price)

Thank You!

## Deficit/GDP and 10y Bond Yields, Spain and the UK



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# Macro Model: Setup and actors

- Three periods
- Bond traders: strategic and noise
- Workers: strategic and noise
- Government (described by a mechanical rule)

[back to setup](#)

# Workers: Preferences and Technology

- Only alive in periods 2 and 3
- Strategic workers
  - ▶ One unit of endowment in period 2
  - ▶ Wish to consume in period 3, risk neutral
  - ▶ Can store good (zero return) or sell it
- Noise workers
  - ▶ (Unobserved) relative mass  $\Phi(\epsilon_2^w)$ ,  $\epsilon_2^w \sim N(0, 1/\psi_2^w)$
  - ▶ Can produce in period 3
  - ▶ Demand 1 unit of consumption in period 2

# Bond Traders: Preferences and Technology

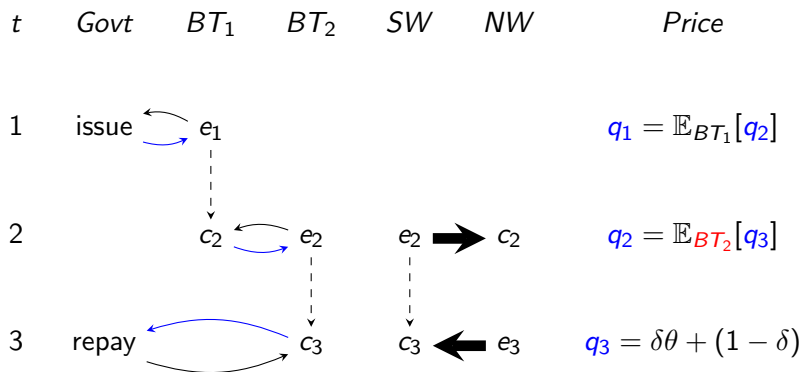
- 2 OLGs living for two periods
- Endowed with goods when young
- Want to consume when old, risk neutral
  
- Strategic traders:
  - ▶ Can store
  - ▶ Can buy one unit of government bonds
  
- Noise traders:
  - ▶ Demand an (unobserved) fraction  $\Phi(\epsilon_t^b)$ ,  $\epsilon_t^b \sim N(0, 1/\psi_t^b)$ , of gov't debt
  
- Mass of bond traders negligible compared to workers



## Government - “Euro” scenario

- Auctions one unit of debt in period 1 (per capita per young strategic trader), price  $q_1$
- Debt is a promise to pay  $\hat{s}(q_1)$  Euros (goods) in period 3. Examples:
  - ▶  $\hat{s}(q_1) \equiv 1$  (Eaton and Gersovitz)
  - ▶  $\hat{s}(q_1) \equiv 1/q_1$  (Calvo)
- In period 3, gov't collects taxes, depending on the realization of  $s \sim N(\mu_0, 1/\alpha_0)$ :
  - ▶ If  $s \geq \hat{s}(q_1)$ , full repayment
  - ▶ Otherwise, haircut  $1 - \theta$ , gov't pays back  $\theta\hat{s}(q_1)$

# Euro Markets



goods; *bonds*; storage (dashed)

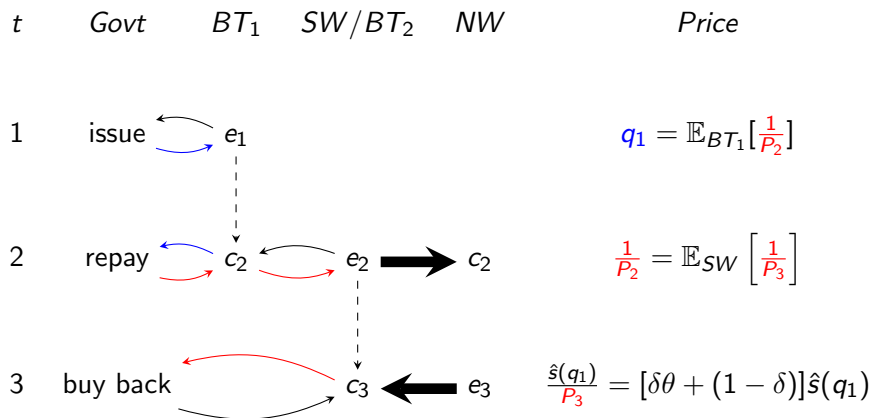
Yen Markets

## Government - “Yen” scenario

- Auctions one unit of debt in period 1 (per capita per young strategic trader), price  $q_1$
- Debt is a promise to pay  $\hat{s}(q_1)$  Yen.
- In period 2, gov't prints Yen, pays debt back.
- In period 3, gov't collects taxes, depending on the realization of  $s \sim N(\mu_0, 1/\alpha_0)$ :
  - If  $s \geq \hat{s}(q_1)$ , collects  $\hat{s}(q_1)$
  - Otherwise, collects  $\theta\hat{s}(q_1)$ } (same as Euro scenario)
- Period-3 taxes used to buy Yen back. Price level is either 1 or  $1/\theta$ .

Price Level Determination

# Yen Markets



goods; *bonds*; *cash*; storage (dashed)

Euro Markets

## Euro vs. Yen: the Key Difference

- Eventual default/inflation is the same at the end ( $t = 3$ )
- Identity of primary-market participants is the same at the start ( $t = 1$ )
- **Period 2** Identity of secondary-market participants different:
  - ▶ Under Euro, bonds offloaded to **new bond traders**
  - ▶ Under Yen, bonds offloaded to **workers (through cash)**
- With same information, same prices/payoffs in the 2 scenarios:
  - ▶ collapse them into a single problem:  $q_2 := 1/P_2$  in the Yen case
  - ▶ index scenarios with period-2 agents' information precision

# Price Level Determination, Yen Economy

Government money valuation equation

$$\frac{M}{P_3} = \text{real tax revenues}$$

and since  $M = \hat{s}(q_1)$  (govt repays debt with money at  $t = 2$ )

$$\frac{M}{P_3} = \frac{\hat{s}(q_1)}{P_3} = \delta \cdot \theta \hat{s}(q_1) + (1 - \delta) \cdot \hat{s}(q_1)$$

so that

$$\begin{cases} \delta = 1 & P_3 = 1/\theta \\ \delta = 0 & P_3 = 1 \end{cases}$$

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# Equilibrium Definition

## Definition

A Perfect Bayesian Equilibrium consists of bidding strategies  $d(x_{i,t}, q_t)$  for strategic players, a price function  $q(s, \epsilon_t)$  and posterior beliefs  $p(x_{i,t}, q_t)$  such that

- (i)  $d(x_{i,t}, q_t)$  is optimal given beliefs  $p(x_{i,t}, q_t)$ ,
- (ii)  $q(s, \epsilon_t)$  clears the market for all  $(s, \epsilon_t)$ , and
- (iii)  $p(x_{i,t}, q_t)$  satisfies Bayes' Law for all market clearing prices  $q_t$ .

## More Definitions

- Precision of first-period posterior beliefs

$$\frac{1}{\gamma_1} := \frac{1}{\alpha_0 + \beta_1(1 + \psi_1)}$$

Case 1:  $t = 1$  beliefs

Case 1: comparative statics

- Second-period Bayesian weights (case with recall)

$$w_{1,S} := \frac{\beta_1 \psi_1}{\alpha_0 + \beta_1 \psi_1 + \beta_2(1 + \psi_2)} \quad w_{2,S} := \frac{\beta_2(1 + \psi_2)}{\alpha_0 + \beta_1 \psi_1 + \beta_2(1 + \psi_2)}$$

Case 2:  $q_1$

- Aggregate noise term of first-period price (case with recall)

$$S := \sqrt{w_{2,S}^2 \left( \frac{1}{\gamma_1} + \frac{1}{\beta_2 \psi_2} \right) + \sigma_S^2}$$

Case 2:  $q_1$

Case 2: comparative statics



# Simplest Case

## Proposition (1)

*There exists a cutoff level  $\hat{z}_1^\beta \in \mathbb{R}$  such that when  $z_1 < \hat{z}_1^\beta$ , a decrease in  $\beta_2$  improves the issuance price  $q_1$ , whereas the reverse occurs for  $z_1 > \hat{z}_1^\beta$ .*

## Proposition (2)

*There exists a cutoff level  $\hat{z}_1^\psi \in \mathbb{R}$  such that when  $z_1 < \hat{z}_1^\psi$ , a decrease in  $\psi_2$  improves the issuance price  $q_1$ , whereas the reverse occurs for  $z_1 > \hat{z}_1^\psi$ .*

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## With Recall, Exogenous Threshold

### Proposition (3)

*There exists a cutoff level  $\hat{z}_1^\psi \in \mathbb{R}$  such that when  $z_1 < \hat{z}_1^\psi$ , a decrease in  $\psi_2$  improves the issuance price  $q_1$ , whereas the reverse occurs for  $z_1 > \hat{z}_1^\psi$ .*

### Proposition (4)

*Assume that  $\psi_2 \geq \psi_1$  and  $\beta_2^A \geq \beta_1$ . Let  $\beta_2^B < \beta_2^A$ . Then there exists a cutoff level  $\hat{z}_1^\beta \in \mathbb{R}$  such that when  $z_1 < \hat{z}_1^\beta$ ,  $q_1$  evaluated at  $\beta_2^A$  is smaller than at  $\beta_2^B$ , whereas the reverse occurs for  $z_1 > \hat{z}_1^\beta$ , holding all other parameters fixed.*

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## With Recall, Endogenous Threshold

### Proposition (5)

*Assume that  $\psi_2 \geq \psi_1$  and  $\beta_2^A \geq \beta_1$ , and let (??) hold. Let  $\beta_2^B < \beta_2^A$ . Then there exist two cutoffs level  $\hat{z}_1^L \leq \hat{z}_1^H \in \mathbb{R}$  such that when  $z_1 < \hat{z}_1^L$ ,  $q_1$  evaluated at  $\beta_2^A$  is smaller than at  $\beta_2^B$ , whereas the reverse occurs for  $z_1 > \hat{z}_1^H$ , holding all other parameters fixed.*

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